Extraction of Airways from CT Data
Using Bayesian Smoothing

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Motivation

- Chronic Obstructive Pulmonary Disease (COPD)
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  - Smoking, Air pollution, Genes
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Diagnosis

- Spirometry
  - Lung function tests
  - Volume of air inhaled & exhaled
    - Patient dependent
    - Low reproducibility
    - Mild cases go unnoticed
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    - Patient dependent
    - Low reproducibility
    - Mild cases go unnoticed
- **3D Chest computed tomography (CT)**
  - Lot more information
    - Arduous to read the data; even for experts
    - Low inter-observer agreement
Objective

Airway tree segmentation from CT to obtain useful COPD biomarkers
Existing Methods

- **Sequential in nature**
  - Like Region-growing based methods
  - Susceptible to local anomalies
  - Acquisition noise / mucous plugs / artifacts
Desired Properties

A stochastic and *exploratory* algorithm that is computationally tractable
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A stochastic and *exploratory* algorithm that is computationally tractable

- Probability densities to capture uncertainties
- Incorporate rich domain knowledge (*priors*)
- Particle filters do exist, but
  - Computationally expensive (volume data, several hundred branches)
  - Track sequentially
Idea
Formulate tree *segmentation* as *Bayesian Tracking* of individual branches
Bayesian Tracking

- Probabilistic state-space approach to tracking
- Strong model-based methods (almost) readily applicable
- State estimation from *a posteriori* density
- Batch data (like CT images) → Bayesian Smoothing
Probabilistic State-space Model

Model

- Airway tree as a set of *independent* branches
  \[ \mathbf{X} = \{\mathbf{X}_1, \ldots, \mathbf{X}_T\} \]
- Each branch as a sequence of state vectors
  \[ \mathbf{X}_i = [\mathbf{x}_0, \mathbf{x}_1, \ldots, \mathbf{x}_l_i] \]
- State vector at each step
  \[ \mathbf{x}_k = [x, y, z, r, v_x, v_y, v_z]^T \]
- Vectorised image data
  \[ \mathbf{Y} = [\mathbf{y}_0, \ldots, \mathbf{y}_T]; \]
  \[ \mathbf{y}_k = [x, y, z, r]^T \]
Objective

To estimate the *a posteriori* distribution:

\[ p(X|Y) \]
Objective

To estimate the \textit{a posteriori} distribution:

\[ p(X|Y) \approx \prod_{i} p(X_i|Y) \]
RTS (Kalman) Smoother

Density per branch, $p(X_i|Y)$, approximated using RTS\textsuperscript{1} Smoother.

- Recursively estimate posterior density
- Closed form, simple-to-compute expressions
- Provides Gaussian density estimates at each step
- Inherent uncertainty estimates

\textsuperscript{1}Rauch-Tung-Striebel
Probabilistic State-space Models

Process Model (Transition Density)

\[ x_k = F x_{k-1} + q \equiv p(x_k|x_{k-1}) \] (1)

**F**: State transition function, \( q \sim N(0, Q) \): Process noise,
\( x_k = [x, y, z, r, v_x, v_y, v_z]^T \)
Probabilistic State-space Models

Process Model (Transition Density)

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\(F\): State transition function, \(q \sim N(0, Q)\): Process noise,
\(x_k = [x, y, z, r, v_x, v_y, v_z]^T\)

Measurement Model (Measurement Likelihood)

\[ y_k = H x_k + m \equiv p(y_k|x_k) \quad (2) \]

\(H\): Measurement function, \(m \sim N(0, R)\): Measurement noise,
\(y_k = [x, y, z, r]^T\)
Validation of Tracked branches

- Exploratory algorithm $\rightarrow$ Several Candidate branches
- Select likely candidates based on tracking confidence

$$\mu_i = \frac{\sum_{k=1}^{l_i} \text{Tr}(P_{k|k})}{l_i}. \quad (3)$$

$P_{k|k}$ is posterior covariance matrix at step $k$.
- Measure of how well tracked branches fit process & meas. models
Data

- Danish Lung Cancer Screening Trial
- Low-dose Chest CT scans
- 32 scans split into Training and Test sets
- Reference consists of expert verified union of results from two previous methods
Application to Airways

- Intensity to Probability Image using trained voxel classifier
- Normalised multi-scale blob detection (Laplacian of Gaussians)
- 3-D Volume Data $\rightarrow$ 4-D Measurement Vector ($\mathbf{y}_k = [x, y, z, r]^T$)
Evaluation: CT Chest Data

In the segmented results, pink surface is the reference segmentation and blue lines correspond to the tracked centerlines.
Evaluation: CT Chest Data

Figure: Input Data, Segmented results before and after thresholding to remove false positive branches.

In the segmented results, pink surface is the reference segmentation and blue lines correspond to the tracked centerlines.
Results

- Error Measure based on centerline distances
- Average of two distances, \( d_{err} = (d_{FP} + d_{FN})/2 \)
- Compared with Region Growing (RG) on Probability image
- RTS+RG: Results from proposed method (RTS) merged with RG

Table 2: Performance comparison on the test set

<table>
<thead>
<tr>
<th>Method</th>
<th>( d_{FP} ) (mm)</th>
<th>( d_{FN} ) (mm)</th>
<th>( d_{err} ) (mm)</th>
<th>Std.Dev. (mm)</th>
</tr>
</thead>
<tbody>
<tr>
<td>RG</td>
<td>0.423</td>
<td>3.579</td>
<td>2.001</td>
<td>0.208</td>
</tr>
<tr>
<td>(RTS+RG)(_1)</td>
<td>0.449</td>
<td>2.102</td>
<td>1.276</td>
<td>0.187</td>
</tr>
<tr>
<td>(RTS+RG)(_2)</td>
<td>0.401</td>
<td>2.658</td>
<td>1.529</td>
<td>0.165</td>
</tr>
</tbody>
</table>

- (RTS+RG)\(_1\): Large improvement in \( d_{err} \) for a small increase in \( d_{FP} \)
- (RTS+RG\(_2\)): Simultaneous improvement in \( d_{FP}, d_{FN} \)
Summary

- Medical images present interesting challenges
- Segmentation of Airways for COPD diagnosis
- Bayesian Tracking presented as a useful approach
- Exploratory algorithm; can overcome local anomalies
- Extract tree as set of branches
- Uncertainty estimates to qualify branches
- Broader applications beyond airways (vessels, neurons etc.)
Questions/ Comments

\[\text{https://en.wikipedia.org/wiki/Tobacco\_\(\text{Last\_Week\_Tonight}\)}\]
Recursive estimation of Mean, Cov.

Table 1: Standard RTS Smoother Equations

<table>
<thead>
<tr>
<th>Forward Filtering</th>
<th>Backward Smoothing</th>
</tr>
</thead>
<tbody>
<tr>
<td>$\hat{x}_{k</td>
<td>k-1} = F\hat{x}_{k-1</td>
</tr>
<tr>
<td>$P_{k</td>
<td>k-1} = FP_{k-1</td>
</tr>
<tr>
<td>$v_{k} = y_{k} - H\hat{x}_{k</td>
<td>k-1}$</td>
</tr>
<tr>
<td>$S_{k} = HP_{k</td>
<td>k-1}H^{T} + R$</td>
</tr>
<tr>
<td>$K_{k} = P_{k</td>
<td>k-1}H^{T}S_{k}^{-1}$</td>
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